



Analyze Example

Input Data – Output Pages 1 to 4

These pages contain the input data as described above under DESIGN, except for the group load data. The column is analyzed and the yield nominal (yield) strength of the column section is determined.

Nominal Strength Values – Output Pages 5 & 6

The angle of the resultant nominal moment varies from 90 degrees (Transverse) to 0 degrees (Longitudinal) in 15 degree increments. The nominal axial load P varies from $0.8P_o$ TO $-0.1P_o$ in increments of $0.1P_o$ (P_o = Nominal Axial load Strength).

The last page in this section is a plot of the nominal moments.



TITLE 4' X 8' RECTANGULAR WITH FILLETS ANALYSIS 7/25/1995 09:50:35 PAGE 1

```
*****  
*                               YIELD PROGRAM - VERSION 1.01    10.11.90                               *  
*****
```

```
COLUMN TYPE                = 1 (RECTANGULAR W/FILLETS)  
CONCRETE LOOPS              = 1  
TOTAL NO. OF CONCRETE COORD. = 8  
STEEL REBAR PATTERN        = 2 (INTERACTING LOOPS)  
NUMBER OF STEEL REBAR LOOPS = 1  
TOTAL NO. OF STEEL REBARS  = 30  
PLOT TYPE                  = 4 (MIN VS. MAX)  
DESIGN TYPE                 = 0 (ANALYSIS)  
PERCENT STEEL LIMITS      = (1.50 * MIN, 6.00 * MAX.)
```

```
*****  
* MATERIAL PROPERTIES *  
*****
```

```
ULTIMATE CONCRETE COMPRESSIVE STRESS - FC = 3000. (PSI)  
YOUNG'S MODULUS FOR CONCRETE          EC = 3249500. (PST)  
YOUNG'S MODULUS FOR STEEL BARS        ES = 29000000. (PSI)  
ULTIMATE CONCRETE COMPRESSIVE STRAIN  ECU = .003 (IN PER IN)  
YIELDING STRESS FOR STEEL BARS        FYS = 60000. (PSI)
```



TITLE 4' x 8' RECTANGULAR WITH FILLETS ANALYSIS 7/25/1998 09:50:33 PAGE 12

RECTANGULAR CROSS-SECTION (WITH FILLETS)

IX	HY	FX	FY
96.00	48.00	9.00	9.00

CONCRETE COORDINATES (IN/IN)

COORD	X	Y
1	48.00	15.00
2	39.00	24.00
3	-39.00	24.00
4	-48.00	15.00
5	-48.00	-15.00
6	-39.00	-24.00
7	39.00	-24.00
8	48.00	-15.00



TITLE 4' X 5' RECTANGULAR WITH PILLETS ANALYSIS 7/25/1995 09:53:19 PAGE 3

INTERSECTING LOOP PATTERN

RADIUS	SPACING	AREA
20.49	24.00	4.58

STEEL REBAR COORDINATES (INCHES)

COORD	X	Y
1	-12.00	16.51
2	12.00	-16.51
3	-18.74	19.80
4	18.74	-19.80
5	-26.18	20.37
6	26.18	-20.37
7	-33.33	18.24
8	33.33	-18.24
9	-39.24	13.70
10	39.24	-13.70
11	-43.33	7.33
12	43.33	-7.33
13	-44.49	.00
14	44.49	.00
15	-43.33	-7.33
16	43.33	7.33
17	-39.24	-13.70
18	39.24	13.70
19	-33.33	-18.24
20	33.33	18.24
21	-26.18	-20.37
22	26.18	20.37
23	-18.74	-19.80
24	18.74	19.80
25	12.00	16.51
26	-12.00	-16.51
27	4.24	20.05
28	-4.24	-20.05
29	-4.24	20.05
30	4.24	-20.05

THE MAIN CONCRETE STRENGTH IS ASSUMED TO BE # 11 BARS



TITLE 4' X 8' RECTANGULAR WITH FILLETS ANALYSIS 7/23/1995 09:50:19 PAGE 14

```
*****
* INITIAL REFERENCE DATA *
*****

TOTAL AREA OF THE SECTION          AG =      30.86 FT**2
NOMINAL AXIAL LOAD STRENGTH       FO = 14980.79 KIPS
TOTAL REINFORCEMENT AREA         AST =      46.80 IN**2
PERCENT STEEL                     *        1.05 %

GROSS MOMENT OF INERTIA ABOUT Y-AXIS IYC =    154.81 FT**4
GROSS MOMENT OF INERTIA ABOUT X-AXIS IKC =     39.19 FT**4

STEEL MOMENT OF INERTIA ABOUT Y-AXIS IYS =     2.0159 FT**4
STEEL MOMENT OF INERTIA ABOUT X-AXIS IXS =     .6197 FT**4
```



TITLE # 3-B RECTANGULAR WITH FILLETS ANALYSIS 9/25/1995 09:50:19 PAGE 5

 * NOMINAL STRENGTH VALUES (KIP+FT) ASD = 46.50 SQ IN *

ANGLE	TRANS MMX	LONG MMX	COMB MMX	AXIAL KN	P-BALANCE (APPROX)
90.0	14510.	0.	14510.	8978.	5534
	18130.	0.	18130.	7479.	
	17020.	0.	17020.	5986.	
	16764.	0.	16764.	4490.	
	15369.	0.	15369.	2994.	
	12886.	0.	12886.	1497.	
	11249.	0.	11249.	748.	
	9348.	0.	9348.	0.	
	7177.	0.	7177.	-747.	
	4758.	0.	4758.	-1495.	
75.0	12563.	3360.	13004.	8975.	8455
	13490.	3658.	14171.	7479.	
	14317.	3797.	14612.	5986.	
	14177.	3795.	14675.	4450.	
	11185.	3523.	13652.	2994.	
	11308.	3626.	11704.	1498.	
	10015.	2691.	10368.	750.	
	8411.	2252.	8707.	0.	
	6554.	1754.	6785.	-747.	
	4412.	1181.	4567.	-1495.	
60.0	8365.	5384.	10802.	8975.	8109
	10220.	5804.	12756.	7479.	
	10554.	6064.	12172.	5986.	
	10920.	6026.	12133.	4487.	
	9798.	5642.	11308.	2994.	
	8440.	4889.	8705.	1498.	
	7464.	4305.	6617.	748.	
	6307.	3638.	7281.	0.	
	4967.	2966.	5735.	-747.	
	3385.	1953.	3908.	-1495.	

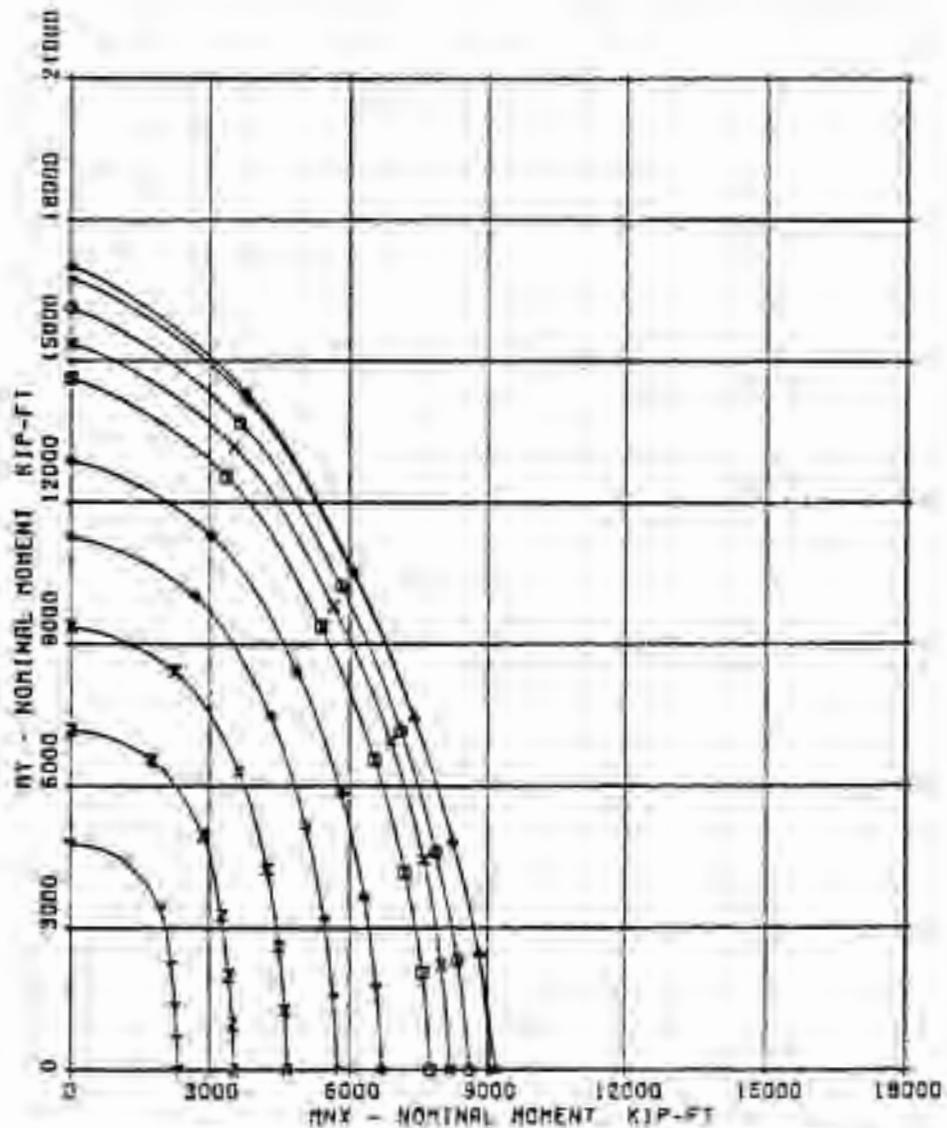
TITLE 8' X 8' RECTANGULAR WITH FILLETS ANALYSIS 7/25/1995 08:50:33 PAGE 6

* NOMINAL STRENGTH VALUES (KIP-FT) AST - A6-50 S11W *

ANGLE	TRANS MOY	LONG MOY	COMB MO	AXIAL BN	P-BALANCE (APPROX)
15.0	8559	8518	9247	8978	5237
	7169	7089	10074	7421	
	7447	7374	10460	3923	
	7431	7281	10460	4428	
	5936	6070	9753	2991	
	3846	5917	8247	1495	
	5102	5076	7197	747	
	4239	4231	5959	1	
	3266	2259	4618	-747	
	2196	2189	3099	-1495	
10.0	8174	7180	8308	8978	5143
	1606	7385	9097	7462	
	4827	6219	9532	3443	
	4831	6227	9541	1468	
	4450	7577	8967	3991	
	3664	8308	7293	1495	
	3171	5467	6313	747	
	2609	4492	5195	-1	
	2989	2423	3958	749	
	2325	2274	2637	-1495	
15.0	2046	7554	7926	8978	5236
	2353	8371	8646	7480	
	2445	8987	9140	5984	
	2445	8799	9133	4088	
	2215	7970	8272	2991	
	2777	8958	6795	1495	
	2530	5647	5931	747	
	2251	4683	4790	-1	
	972	4500	3633	-747	
	643	2312	2401	-1495	
0	0	7719	7719	8975	5453
	0	6589	8589	7279	
	0	9188	9188	5963	
	0	9080	9050	4430	
	0	8171	8171	2493	
	0	6688	6628	1887	
	0	5742	5742	749	
	0	4678	4678	1	
	0	3538	3538	-747	
	0	2329	2329	-1495	

4' X 8' RECTANGULAR WITH FILLETS ANALYZE
 AST = 46.83 50 IN PMAX = 14980 K
 FC = 3.25 KSI FY = 60 KSI EO = 0.003

1	P	=	8976	K
2	P	=	7485	K
3	P	=	6884	K
4	P	=	6480	K
5	P	=	6207	K
6	P	=	6027	K
7	P	=	5924	K
8	P	=	5880	K
9	P	=	5840	K
10	P	=	5800	K
11	P	=	5760	K
12	P	=	5720	K
13	P	=	5680	K
14	P	=	5640	K
15	P	=	5600	K
16	P	=	5560	K
17	P	=	5520	K
18	P	=	5480	K
19	P	=	5440	K
20	P	=	5400	K
21	P	=	5360	K
22	P	=	5320	K
23	P	=	5280	K
24	P	=	5240	K
25	P	=	5200	K
26	P	=	5160	K
27	P	=	5120	K
28	P	=	5080	K
29	P	=	5040	K
30	P	=	5000	K
31	P	=	4960	K
32	P	=	4920	K
33	P	=	4880	K
34	P	=	4840	K
35	P	=	4800	K
36	P	=	4760	K
37	P	=	4720	K
38	P	=	4680	K
39	P	=	4640	K
40	P	=	4600	K
41	P	=	4560	K
42	P	=	4520	K
43	P	=	4480	K
44	P	=	4440	K
45	P	=	4400	K
46	P	=	4360	K
47	P	=	4320	K
48	P	=	4280	K
49	P	=	4240	K
50	P	=	4200	K
51	P	=	4160	K
52	P	=	4120	K
53	P	=	4080	K
54	P	=	4040	K
55	P	=	4000	K
56	P	=	3960	K
57	P	=	3920	K
58	P	=	3880	K
59	P	=	3840	K
60	P	=	3800	K
61	P	=	3760	K
62	P	=	3720	K
63	P	=	3680	K
64	P	=	3640	K
65	P	=	3600	K
66	P	=	3560	K
67	P	=	3520	K
68	P	=	3480	K
69	P	=	3440	K
70	P	=	3400	K
71	P	=	3360	K
72	P	=	3320	K
73	P	=	3280	K
74	P	=	3240	K
75	P	=	3200	K
76	P	=	3160	K
77	P	=	3120	K
78	P	=	3080	K
79	P	=	3040	K
80	P	=	3000	K
81	P	=	2960	K
82	P	=	2920	K
83	P	=	2880	K
84	P	=	2840	K
85	P	=	2800	K
86	P	=	2760	K
87	P	=	2720	K
88	P	=	2680	K
89	P	=	2640	K
90	P	=	2600	K
91	P	=	2560	K
92	P	=	2520	K
93	P	=	2480	K
94	P	=	2440	K
95	P	=	2400	K
96	P	=	2360	K
97	P	=	2320	K
98	P	=	2280	K
99	P	=	2240	K
100	P	=	2200	K





Input Data Format (XEDIT)

General Data

Header - (A40,I4X,I1)

Columns	Entry	Variable
1 - 40	Project Title	HEAD
55	Version (enter 1)	IVERS

Column Type - (I10)

Columns	Entry	Variable
1 - 10	Column Type (1,2,3,4,6,8,9)	ICON

Column Data - (2I10)

This line required for manual input (type = 1) only.

Columns	Entry	Variable
1 - 10	Number of Concrete Boundary Loops	NSLOOP
11 - 20	Total Number of Concrete Coordinates	NNODE

Rebar Type - (I10)

Columns	Entry	Variable
1 - 10	Rebar Type (1,2,3,4,5)	IREBAR

Rebar Data - (2I10)

Columns	Entry	Variable
1 - 10	Number of Steel Loops or Rows	NSLOOP
11 - 20	Total Number of Steel Rebars	NBAR

Plot Type - (I10)

Columns	Entry	Variable
1 - 10	Plot Type (0 to 4)	IPLOT

Problem Type, Steel Limits, Spiral Reinforcement (110,2F10.0,110,3F10.0)

Columns	Entry	Variable	Units
1 - 10	Problem Type	IPROB	
11 - 20	Minimum Percent Longitudinal Steel	RMIN	%
21 - 30	Maximum Percent Longitudinal Steel	RMAX	%
31 - 40	Number of Columns in Bent	NC	
41 - 50	Out to Out Diameter of Spiral	DSO	ft
51 - 60	Distance from Top Plastic Hinge to Center of Gravity of Superstructure	CGS	ft
61 - 70	Center to Center Spacing of Columns	CSP	ft

Material Properties - (4F10.0)

Columns	Entry	Variable	Units
1 - 10	ULT Concrete Compressive Stress	FC	Psi
11 - 20	Young's Modulus for Steel Rebars	ES	Psi
21 - 30	ULT Concrete Compressive Strain	EO	In/In
31 - 40	Yielding Stress for Steel Rebars	FS	Psi

Column Dimensions

Concrete Coordinates - Manual Input (type = 1) (2F10.0,110)

Note: Repeat this series of lines for each separate concrete boundary loop.

1st line (2F10.0,110)

Columns	Entry	Variable	Units
1 - 10	X-Coordinate	X(I)	ft
11 - 20	Y-Coordinate	Y(I)	ft
21 - 30	Number of Coordinates this Loop	LNODE(NLOOP)	

I = 1 to LNODE(NLOOP)

One line for each remaining coordinate (2F10.0).

Do not repeat the number of coordinates in the loop.



Column Dimensions (Types 2,3,4,6,8,9) - (4F10.0)

Columns	Entry	Variable	Units
1 - 10	X-Width	BX	In
11 - 20	Y-Thickness	HY	In
21 - 30	X-Fillet	FX	In
31 - 40	Y-Fillet	FY	In

Rebar Layouts

Steel Coordinates - Manual Input (Type = 1) (2F10.0,20X,F10.0,110)

Note: Repeat this series of lines for each separate steel loop.

1st Line (2F10.0,20X,F10.0,110)

Columns	Entry	Variable	Units
1 - 10	X-Coordinate	XS(I)	In
11 - 20	Y-Coordinate	YS(I)	In
41 - 50	Area of Steel	AS(I)	Sq In
51 - 60	Number of Coordinates this Loop	LSNODE(NSLOOP)	

I = 1 to LSNODE(NSLOOP)

One line for each remaining rebar coordinate (2F10.0)

Do not repeat the number of coordinates in the loop.

Rebar Layout

Intersecting Loops (Type 2) - (2F10.0,20X,1F10.0)

Semicircular Ends (Type 3) - (2F10.0,20X,1F10.0)

Concentric Loops (Type 4) - (1F10.0,30X,1F10.0,110)

Note: For concentric loops (type 4) the number of lines in this section is equal to the "Total Number of Loops".

I = 1 to NSLOOP

Columns	Entry	Variable	Units
1 - 10	Loop Radius	RS(I)	In
11 - 20	Loop Spacing	SPACE	In
21 - 30	Area of Each Bar	AS(I)	Sq In
31 - 40	Number of Bars in this Loop	LSNODE(I)	



Rebar Layouts - Rows (Type 5) - (5F10,0,110)

Note: The number of lines in this section is equal to the "Total Number of Rows".
I = J to NSLOOP

Columns	Entry	Variable	Units
1 - 10	X-Coordinate Start Row	X1(I)	ft
11 - 20	Y-Coordinate Start Row	Y1(I)	ft
21 - 30	X-Coordinate End Row	X2(I)	ft
31 - 40	Y-Coordinate End Row	Y2(I)	ft
41 - 50	Area of Each Bar	AS(I)	ft ²
51 - 60	Number of Bars in this Row	LSNODE(J)	

Load Data - Units Kips & Feet - (11 Lines)

Note: You may repeat this section (11 lines) for up to 10 different loadings.

Header - (3A8,A6,7X,A3,4X,A6)

Columns	Entry	Variable Name
1 - 30	Load Name	LOADNO(I)
38 - 40	Create a Footing File? (Yes/No)	PRNT
45 - 50	Footing Type (SPREAD/PILE)	FTYPE

Data - (2F5,0,10X,2F10,0,215,F10,0)

Columns	Entry	Variable	Units
1 - 5	Effective Length Factor Transverse	Ky	
6 - 10	Effective Length Factor Longitudinal	Ks	
21 - 30	Percent Live Load Impact	PERI	%
31 - 40	Column Length	ZLEN	ft
41 - 45	Tie = 1, Spiral = 0 (Confinement)	ITIE	
46 - 50	Top = 1, Bottom = 0 (Load Connection)	ITOP	
51 - 60	Seismic Ductility and Risk Factor	Z	



Column End Conditions (61X,411)

Columns	Entry	Variable
62	Top Transverse	Topy
63	Top Longitudinal	Topx
64	Bottom Transverse	Boty
65	Bottom Longitudinal	Botx

Service Loads – 3(F7.0,F8.0,4F7.0,4F6.0)

1st Line	My	Transverse Moment
2nd Line	Mx	Longitudinal Moment
3rd Line	N	Axial Load

Columns	Entry	Variable Name		
		Line Number		
		1	2	3
1 - 7	Dead Load	DLT	DLI	DLN
8 - 15	PS (Pre Stress)	PST	PSL	PSN
16 - 22	Live Load + Impact (My Max)	HTT	HTL	HTN
23 - 29	Live Load + Impact (Mx Max)	HLT	HLL	HLN
30 - 36	Live Load + Impact (N Max)	HAT	HAL	HAN
37 - 43	W (Wind)	WT	WL	WN
44 - 49	WL (Wind on Live Load)	WLT	WLL	WLN
50 - 55	LF (Longitudinal Force)	LFT	LFL	LFN
56 - 61	CF (Centrifugal Force)	HCFT	HCFL	HCFN
62 - 67	T (Temperature)	TI	TL	TN

P-Loads – 3(15X,3F7.0,19X,F6.0)

1st Line	PMy	Transverse Moment
2nd Line	PMx	Longitudinal Moment
3rd Line	PN	Axial Load

Columns	Entry	1	2	3
16 - 22	Live Load + Impact (PMy Max)	PTT	PTL	PTN
24 - 29	Live Load + Impact (PMx Max)	PLT	PLL	PLN
30 - 36	Live Load + Impact (PN Max)	PAT	PAL	PAN
56 - 61	CF (Centrifugal Force)	PCFT	PCFL	PCFN

*Unreduced Seismic & Arbitrary Loads - 3(6/10.0)*

1st Line My Transverse Moment
2nd Line Mx Longitudinal Moment
3rd Line N Axial Load

Column	Entry	Variable Name		
		Line Number		
		1	2	3
1 - 10	Unreduced Seismic Case 1 Max Trans	EQT1	EQTL	EQTN
11 - 20	Unreduced Seismic Case 2 Max Long	EQL1	EQLL	EQLN
21 - 30	Arbitrary Service AL-1	MYS1	MXS1	PS1
31 - 40	Arbitrary Service AL-2	MYS2	MXS2	PS2
41 - 50	Arbitrary Factored AL-1	MYF1	MXF1	PF1
51 - 60	Arbitrary Factored AL-2	MYF2	MXF2	PF2

Appendix A – Slenderness Effects

The YIELD program calculates the critical buckling load and moment magnification factor based on the unbraced AASHTO design procedure, as described in article 8.16.5 of the CALTRANS *Bridge Design Practice Manual*.

Moment Magnification

The method is based on the moment magnifier concept in which the moments computed by an ordinary frame analysis are multiplied by a moment magnifier. This magnifier, (δ), is a function of the factored axial load, (P_u), and the critical buckling load, (P_c), for the column:

$$M_c = \delta M_2 \quad (8-40)$$

$$\delta = \frac{C_m}{1 - P_u/P_c} \geq 1.0 \quad (8-41)$$

Where: $C_m = 1.0$ for an unbraced frame:

M_c = Design moment

M_2 = Larger end moment

Critical Buckling Load – P_c

The effective length factor (k), the unbraced column length (L_u) and the column stiffness parameter (EI), are used to calculate the critical buckling load (P_c):

$$P_c = \frac{\pi^2 EI}{(k L_u)^2} \quad (8-42)$$

The program determines the effective length factor (k) by using equations (C) and (D) from the AASHTO commentary (1):

for $G_a < 2$:

$$k = \frac{20 - G_a}{20} \sqrt{1 + E_m} \quad (\text{Eq. E})$$



for $G_a > 2$:

$$k = .9 \times \sqrt{1 + G_a} \quad (\text{Eq. D})$$

where (G_a) is the average of the (G) values at the two ends of the column and (G) is:

$$G = \frac{\text{Sum EI/Lc}}{\text{Sum EI/L}} \quad \begin{array}{l} \text{Column} \\ \text{Members in plane at one end of column} \end{array}$$

The (G) values are determined by using the moment distribution factors at the top and bottom of the column.

For members hinged at one end and fixed at the other the effective length factor (k) is taken as 2.1.

Stiffness Parameter – EI

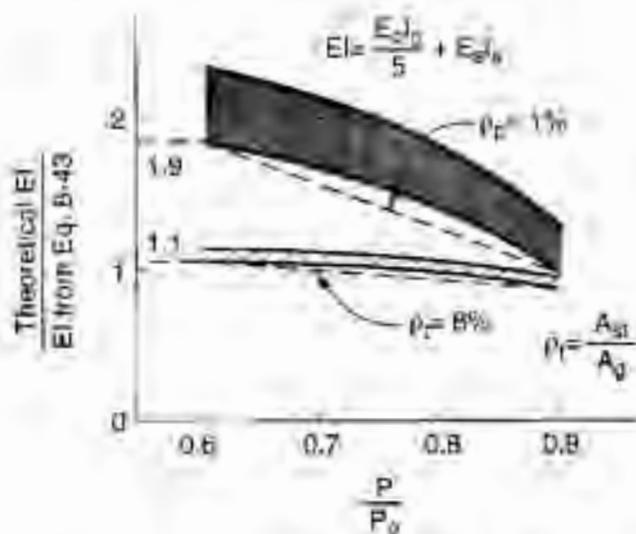
The AASHTO procedure approximates stiffness variations due to cracking, creep, and the nonlinearity of the concrete stress-strain curve. Creep due to sustained loads tends to reduce the effective value of EI. This is taken into account by dividing EI by $(1 + B_d)$ where B_d is the ratio of dead load moment to total load moment.

$$EI = (E_c I_g / 5 + E_s I_s) / (1 + B_d) \quad (8-43)$$

Based on information from the ACI Commentary (1), the YIELD program makes a further modification to the stiffness parameter, (EI), depending on the percent steel and the axial load ratio, (P/P_o) (see Figure 1). Most CALTRANS bridge columns have an axial load ratio, (P/P_o) , less than 0.6. For steel ratios of 1 to 8 percent with axial load ratios, (P/P_o) , less than 0.6, the theoretical (EI) varies from 1.9 to 1.1 times greater than that calculated by the AASHTO equation (8-44). For 1 to 8 percent steel with (P/P_o) equal to 0.9 the theoretical and calculated (EI) are about the same. Straight line interpolation is used for steel ratios and axial load ratios that fall between these boundaries, as shown in Figure 1. The net effect is to increase the column stiffness, EI, and thus reduce the amount of moment magnification.

The effects of slenderness are neglected by the program, when the slenderness ratio, (kL/r) , is less than 22 (8.16.5.2.5). When (kl/r) is greater than 100, the YIELD program warns the user to either redesign the column with a larger cross section or perform a special second order analysis (8.16.5.2.6).

The program neglects moment magnification for Group VII seismic loads. By definition the plastic moment is the capacity of the column and the moment cannot be magnified.



**Equation of Flexural Stiffness vs. Theoretical Values
Figure 1**

Notations

- B_d = Ratio of maximum dead load moment to maximum total load moment, always positive (8.16.5.2.7)
- E_c = Modulus of elasticity of concrete (8.7.1)
- EI = Flexural stiffness of compression member (8.16.5.2.7)
- E_s = Modulus of elasticity of reinforcement (8.7.2)
- I_g = Moment of inertia of gross concrete section about centroidal axis, neglecting reinforcement
- I_s = Moment of inertia of reinforcement about centroidal axis of member cross section
- k = Effective length factor for compression members (8.16.5.2.3)
- L_u = Unsupported length of compression member (8.16.5.2.1)
- M_c = Moment for design of compression member (8.16.5.2.7)
- M_2 = Larger end moment on compression member (8.16.5.2.4)
- P_c = Critical load (8.16.5.2.7)
- P_0 = Nominal axial load strength of a section at zero eccentricity (8.16.4.2.1)
- P_u = Factored axial load at given eccentricity
- δ = Moment magnifier (8.16.5.2.9)
- δ_b = Moment magnifier for members braced against sidesway
- δ_s = Moment magnifier for members not braced against sidesway

References

1. ACI Committee 318, "Commentary on Building Code Requirements for Reinforced Concrete (ACI 318-83)," American Concrete Institute, 1983